

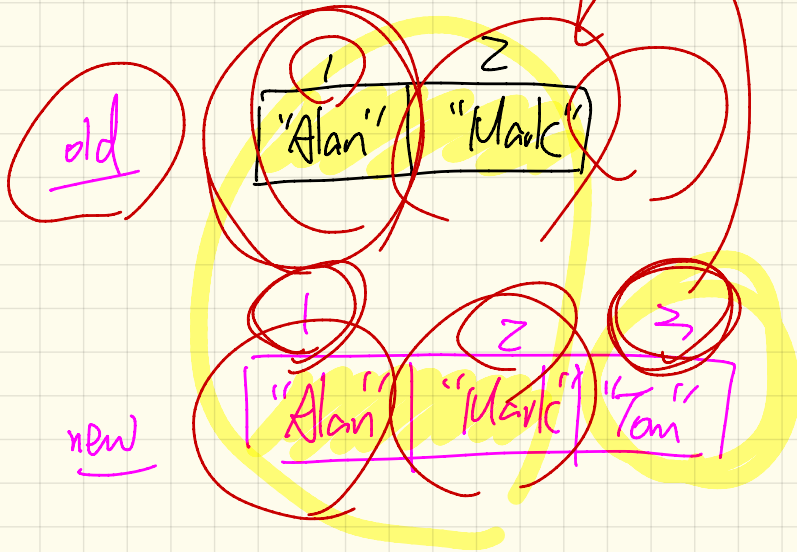
Monday February 11

Lecture 10

Sl

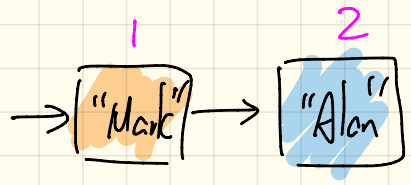
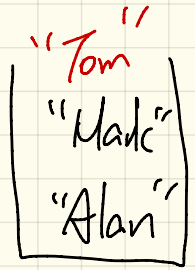
"Mark"
"Alan"

push ("Tom")

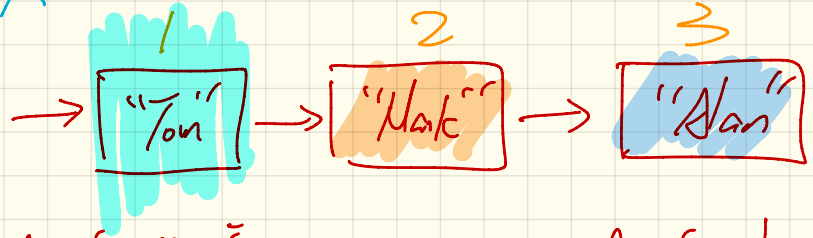


Sz

list first
" "
list[i]
old



list lower upper
new X



Q: empty collection?

push("Tom")

across (2) .. | count as i
all

[imp [i.item] ~
end (dd imp.d-t) [i.item-1]

across all | count as i

across

count 1.. |

as i X

end [count - i.item]

Developing a LIFO Stack

```

class LIFO_STACK[G] create make
feature {NONE} -- Strategy 1: array
imp: ARRAY[G]
feature -- Initialization
make do create imp.make_empty ensure imp.count = 0 end
feature -- Commands
push(g: G)
do [imp.force(g, imp.count + 1)]
ensure
changed: imp[count] ~ g
unchanged: across 1 |..| count - 1 as i all
imp[i.item] ~ (old imp.deep_twin[i.item]) end
end
pop
do [imp.remove_tail(1)]
ensure
changed: count = old count - 1
unchanged: across 1 |..| count as i all
imp[i.item] ~ (old imp.deep_twin[i.item]) end
end

```

not only
 imp. but also
 contracts must
 be modified
 accord. to
 violates

```

class LIFO_STACK[G] create make
feature {NONE} -- Strategy 3: linked-list last item as top
imp: LINKED_LIST[G]
feature -- Initialization
make do create imp.make ensure imp.count = 0 end
feature -- Commands
push(g: G)
do imp.extend(g)
ensure
changed: imp.last ~ g
unchanged: across 1 |..| count - 1 as i all
imp[i.item] ~ (old imp.deep_twin[i.item]) end
end
pop
do imp.finish ; imp.remove
ensure
changed: count = old count - 1
unchanged: across 1 |..| count as i all
imp[i.item] ~ (old imp.deep_twin[i.item]) end
end

```

```

class LIFO_STACK[G] create make
feature {NONE} -- Strategy 2: linked-list first item as top
imp: LINKED_LIST[G]
feature -- Initialization
make do create imp.make ensure imp.count = 0 end
feature -- Commands
push(g: G)
do [imp.put_front(g)]
ensure
changed: imp.first ~ g
unchanged: across 2 |..| count as i all
imp[i.item] ~ (old imp.deep_twin[i.item]) end
end
pop
do [imp.start ; imp.remove]
ensure
changed: count = old count - 1
unchanged: across 1 |..| count as i all
imp[i.item] ~ (old imp.deep_twin[i.item + 1]) end
end

```

class C

imp : {NONE} ? ?

f1

ensure

imp \rightarrow imp

f2

ensure

imp \rightarrow imp

end

class C

imp: {wolves
? ?

model: FUN
do: [hash table] [AVL tree]
end

f1

ensure

imp

model

f2

ensure

imp

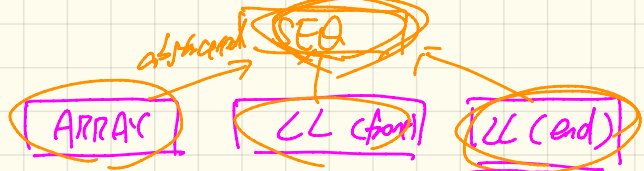
model

end

Using MATHMODELS Library

Implementing Abstraction Function

```
class LIFO_STACK[G -> attached ANY] create make
feature {NONE} -- Implementation (CS3)
imp: LINKED_LIST[G]
feature -- Abstraction function of the stack ADT
model: SEQ[G]
do create Result.make_empty
[across imp as cursor loop Result.append(cursor.item) end]
end
```

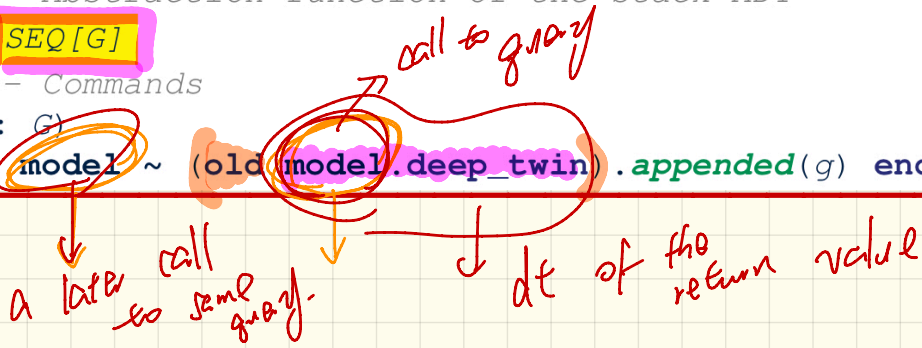


Seq Model

end of seq
is the top

Writing Contracts using Abstraction Function

```
class LIFO_STACK[G -> attached ANY] create make
feature -- Abstraction function of the stack ADT
model: SEQ[G]
feature -- Commands
push (g: G)
ensure model ~ (old(model.deep_twin).appended(g) end
```



```

class LIFO_STACK[G -> attached ANY] create make
feature {NONE} -- Implementation Strategy 1
  imp: ARRAY[G]
feature -- Abstraction function of the stack ADT
  model: SEQ[G]
  do create Result.make_from_array (imp)
  ensure
    counts: imp.count = Result.count
    contents: across 1 |..| Result.count as i all
      Result[i.item] ~ imp[i.item]
  end
feature -- Commands
  make do create imp.make_empty ensure model.count = 0 end
  push (g: G) do imp.force(g, imp.count + 1)
  ensure pushed: model ~ (old model.deep.twin).appended(g) end
  pop do imp.remove_tail(1)
  ensure popped: model ~ (old model.deep.twin).front end
end

```

```

class LIFO_STACK[G -> attached ANY] create make
feature {NONE} -- Implementation Strategy 2 (first as top)
  imp: LINKED_LIST[G]
feature -- Abstraction function of the stack ADT
  model: SEQ[G]
  do create Result.make_empty
  across imp as cursor loop Result.prepend(cursor.item) end
  ensure
    counts: imp.count = Result.count
    contents: across 1 |..| Result.count as i all
      Result[i.item] ~ imp[count - i.item + 1]
  end
feature -- Commands
  make do create imp.make ensure model.count = 0 end
  push (g: G) do imp.put_front(g)
  ensure pushed: model ~ (old model.deep.twin).appended(g) end
  pop do imp.start ; imp.remove
  ensure popped: model ~ (old model.deep.twin).front end
end

```

```

class LIFO_STACK[G -> attached ANY] create make
feature {NONE} -- Implementation Strategy 3 (last as top)
  imp: LINKED_LIST[G]
feature -- Abstraction function of the stack ADT
  model: SEQ[G]
  do create Result.make_empty
  across imp as cursor loop Result.append(cursor.item) end
  ensure
    counts: imp.count = Result.count
    contents: across 1 |..| Result.count as i all
      Result[i.item] ~ imp[i.item]
  end
feature -- Commands
  make do create imp.make ensure model.count = 0 end
  push (g: G) do imp.extend(g)
  ensure pushed: model ~ (old model.deep.twin).appended(g) end
  pop do imp.finish ; imp.remove
  ensure popped: model ~ (old model.deep.twin).front end
end

```


Implementing a LIFO Stack

"tom"
"mark"
"alan"

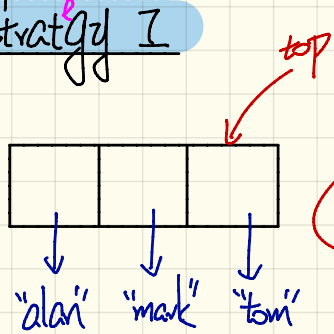
class LIFO_STACK[...]

imp: LL[G] - SZ

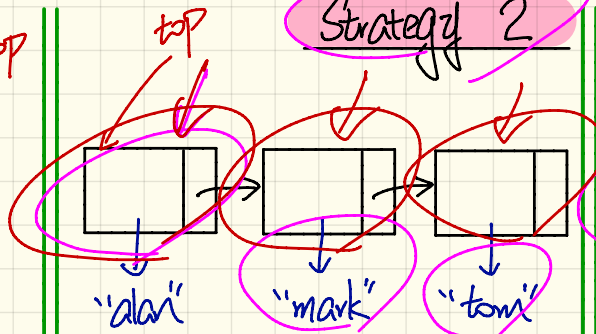
model: SEQ[G]

do
 create Result, make_empty
 → across Imp as cursor
 end
 and Result append
 prepend

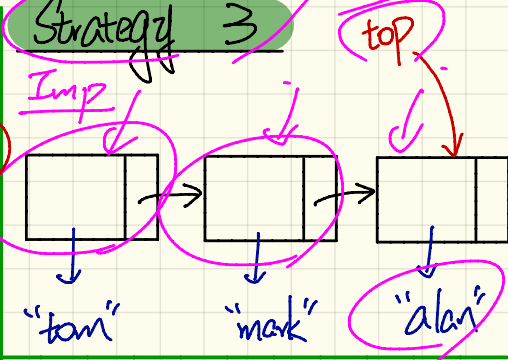
Strategy 1



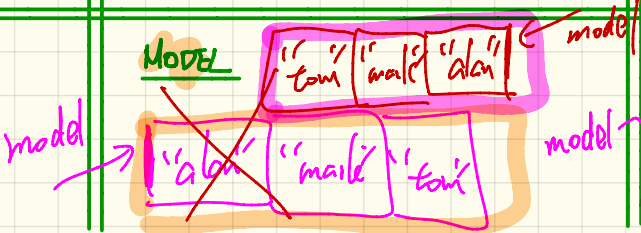
Strategy 2



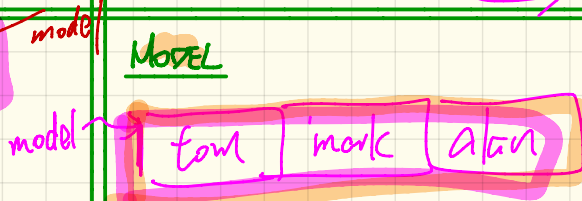
Strategy 3



MODEL



MODEL



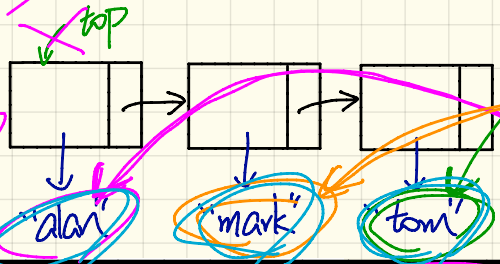
Checking MATH MODELS Contracts at Runtime

Strategy 2

alan
mark
tom

Pre-State

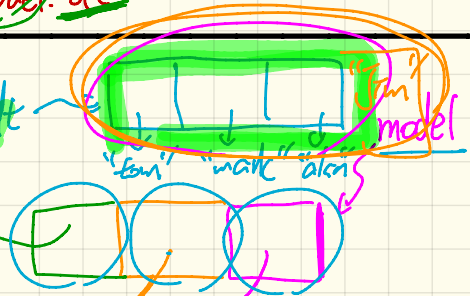
Implementation



model.dt.

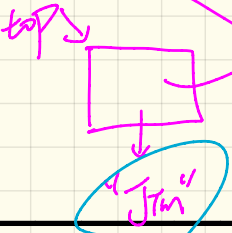
Model

model.dt.

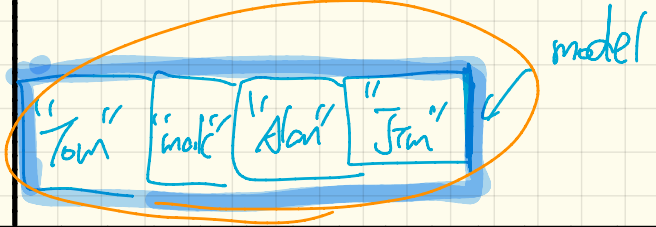


s.push("Jim")

Post-State



Immutable Query



push (g: G)

```
ensure model ~ (old model.deep_twin).appended(g) end
```

← query

Strategy 1: Mathematical Abstraction

'push(g: G)' feature of LIFO_STACK ADT

public (client's view)

old model: SEQ[G]

model ~ (old model.deep_twin).appended(g)

model: SEQ[G]

abstraction function
convert the current *array*
into a math sequence

convert the current *array*
into a math sequence
abstraction function

old imp: ARRAY[G]

imp.force(g, imp.count + 1)

imp: ARRAY[G]

private/hidden (implementor's view)

Strategy 2. Mathematical Abstraction

'push(g: G)' feature of LIFO_STACK ADT

public (client's view)

// *darrrrr!*

old model: SEQ[G]

model \sim (old model.deep_twain).appended(g)

model: SEQ[G]

abstraction function
convert the current *linked list*
into a math sequence

convert the current *linked list*
into a math sequence
abstraction function

old imp: LINKED_LIST[G]

imp.put_front(g)

imp: LINKED_LIST[G]

private/hidden (implementor's view)